## SCIENTIFIC NOTATION

## HOW TO WRITE SCIENTIFIC NOTATION

## SCIENTIFIC NOTATION

Scientific notation is used to write very large or very small numbers such as

- the width of a human hair, 0.000008 m , which is also written as $8 \times 10^{-6} \mathrm{~m}$
- the number of hairs on a human scalp, 100000 ,
 which is also written as 1
$\times 10^{5}$ hairs



## Writing Numbers in Scientific Notation

- A number written in scientific notation contains a coefficient and a power of ten.

$$
\begin{array}{ccc}
\text { coefficient } & \begin{array}{c}
\text { power } \\
\text { of ten }
\end{array} & \text { unit } \\
1.5 \times 10^{2} & \mathrm{~m}
\end{array}
$$

- The coefficient is at least 1 but less than 10 .



## Writing Numbers in Scientific Notation

- The number of spaces moved to obtain a coefficient between 1 and 10 is shown as a power of ten.

52000 . $=5.2 \times 10^{4}$
move decimal 4 spaces left
$0.00378=3.78 \times 10^{-3}$
move decimal 3 spaces right

## Some Powers of Ten

table 2.2 Some Powers of 10

| Number | Multiples of $\mathbf{1 0}$ | Scientific Notation |  |
| ---: | :--- | :---: | :--- |
| 1000 | $10 \times 10 \times 10$ | $1 \times 10^{3}$ |  |
| 100 | $10 \times 10$ | $1 \times 10^{2}$ | Some positive <br> 10 |
| 10 | $1 \times 10^{1}$ | powers of 10 |  |
| 1 | 0 | $1 \times 10^{0}$ |  |
| 0.1 | $\frac{1}{10}$ | $1 \times 10^{-1}$ |  |
| 0.01 | $\frac{1}{10} \times \frac{1}{10}=\frac{1}{100}$ | $1 \times 10^{-2}$ | Some negative <br> powers of 10 |
| 0.001 | $\frac{1}{10} \times \frac{1}{10} \times \frac{1}{10}=\frac{1}{1000}$ | $1 \times 10^{-3}$ |  |

## Comparing Numbers in Standard and Scientific Notation

## Standard Format Scientific Notation

Diameter of the Earth
$12800000 \mathrm{~m} \quad 1.28 \times 10^{7} \mathrm{~m}$

Mass of a human
68 kg
$6.8 \times 10^{1} \mathrm{~kg}$

Diameter of a virus
$0.0000003 \mathrm{~cm} \quad 3 \times 10^{-7} \mathrm{~cm}$

## To write a number in scientific notation:

1. Move the decimal to the right of the first non-zero number.
2. Count how many places the decimal had to be moved.
3. If the decimal had to be moved to the right, the exponent is negative.
4. If the decimal had to be moved to the left, the exponent is positive.

## Learning Check

## Write the following number in the correct scientific notation, 0.000058 g .

## Solution

Write the following number in the correct scientific notation, 0.000058 g .
Step 1 Move the decimal point to obtain a coefficient that is at least 1 but less than 10. $0.000058 \longrightarrow 5.8$
(The decimal moves 5 places to the right, giving a coefficient of 5.8)

## Solution

Write the following number in the correct scientific notation, 0.000058 g .
Step 2 Express the number of places moved as a power of 10 .
Moving the decimal 5 places to the right gives a power of -5 .

## Solution

Write the following number in the correct scientific notation, 0.000058 g .
Step 3 Write the product of the coefficient multiplied by the power of 10 with the unit.
$5.8 \times 10^{-5} \mathrm{~g}$

## Learning Check

Select the correct scientific notation for each.

1. 0.000008
(a) $8 \times 10^{6}$
(b) $8 \times 10^{-6}$
(c) $0.8 \times 10^{-5}$
2. 72000
(a) $7.2 \times 10^{4}$
(b) $72 \times 10^{3}$
(c) $7.2 \times 10^{-4}$

## Solution

Select the correct scientific notation for each.

1. 0.000008
(Move the decimal 6 places to right.)
(b) $8 \times 10^{-6}$
2. 72000
(Move the decimal 4 places to the left.)
(a) $7.2 \times 10^{4}$

## Learning Check

Write each as a standard number.

1. $2.0 \times 10^{-2}$
(a) 200
(b) 0.0020
(c) 0.020
2. $1.8 \times 10^{5}$
$\begin{array}{ll}\text { (a) } 180000 & \text { (b) } 0.000018 \text { (c) } 18000\end{array}$

## Solution

Write each as a standard number.

1. $2.0 \times 10^{-2}$
(c) 0.020
2. $1.8 \times 10^{5}$
(a) 180000

## To write a number in scientific notation:

1. Move the decimal to the right of the first non-zero number.
2. Count how many places the decimal had to be moved.
3. If the decimal had to be moved to the right, the exponent is negative.
4. If the decimal had to be moved to the left, the exponent is positive.

## Express the following in Scientific Notation

|  | PROBLEMS |
| :--- | :--- |
| 1) | .00012 |
| 2) | 1000 |
| 3) | 0.01 |
| 4) | 12 |
| 5) | .987 |
| 6) | 596 |
| 7) | .0000007 |
| 8) | $1,000,000$ |
| 9) | .001257 |
| 10) $987,653,000,000$ |  |
| 11) 8 |  |

ANSWERS

## Express the following in Scientific Notation

| PROBLEMS | ANSWERS |
| :---: | :---: |
| 1) .00012 | 1) $1.2 \times 10^{-4}$ |
| 2) 1000 | 2) $1 \times 10^{3}$ |
| 3) 0.01 | 3) $1 \times 10^{-2}$ |
| 4) 12 | 4) $1.2 \times 10^{1}$ |
| 5) .987 | 5) $9.87 \times 10^{-1}$ |
| 6) 596 | 6) $5.96 \times 10^{2}$ |
| 7) .0000007 | 7) $7.0 \times 10^{-7}$ |
| 8) $1,000,000$ | 8) $1.0 \times 10^{6}$ |
| 9) .001257 | 9) $1.26 \times 10^{-3}$ |
| 10) $987,653,000,000$ | 10) $9.88 \times 10^{11}$ |
| 11) 8 | 11) $8 \times 10^{0}$ |

## Express the following as whole numbers or decimals

|  | PROBLEMS |
| :--- | :--- |
| 1) | $4.9 \times 10^{2}$ |
| 2) | $3.75 \times 10^{-2}$ |
| 3) | $5.95 \times 10^{-4}$ |
| 4) | $9.46 \times 10^{3}$ |
| 5) $3.87 \times 10^{1}$ |  |
| 6) | $7.10 \times 10^{0}$ |
| 7) | $8.2 \times 10^{-5}$ |

ANSWERS

1) $4.9 \times 10^{2}$
2) $3.75 \times 10^{-2}$
3) $5.95 \times 10^{-4}$
4) $9.46 \times 10^{3}$
5) $3.87 \times 10^{1}$
6) $7.10 \times 10^{0}$
7) $8.2 \times 10^{-5}$

## Express the following as whole numbers or decimals

| PROBLEMS | ANSWERS |
| :--- | :--- |
| 1) $4.9 \times 10^{2}$ | 1) 490 |
| 2) $3.75 \times 10^{-2}$ | 2) .0375 |
| 3) $5.95 \times 10^{-4}$ | 3) .000595 |
| 4) $9.46 \times 10^{3}$ | 4) 9460 |
| 5) $3.87 \times 10^{1}$ | 5) 38.7 |
| 6) $7.10 \times 10^{0}$ | 6) 7.10 |
| 7) $8.2 \times 10^{-5}$ | 7) .000082 |

## Guide to Writing a Number in Scientific Notation

| Guide to Writing a Number in |
| :--- |
| Scientific Notation |
| Move the decimal point |
| to obtain a coefficient |
| that is at least 1 but less |
| than 10 . |


| Express the number of |
| :--- |
| places moved as a power |
| of 10 . |
| the poeficient multiplied by of 10 with the |
| unit. |

## Questions



Prepared and Compiled from various sources by
D. Leonard (Learning Specialist)

The Academic Support Center @ Daytona State College
http://www.daytonastate.edu/asc/ascsciencehandouts.html

