

# Graphing a Basic Logarithmic Equation

( using the inverse of a logarithm )

First, keep in mind that logarithm equations and exponential equations are inverses of each other .

Example:  $y = \log_2 x$  is the inverse of  $y = 2^x$

Notice:  $y = \log_2 x$  ← Do you see  $y = 2^x$ ?

This is a convenient way to find the equation of the inverse of a logarithm (i.e., an exponential equation).

## Practice:

Logarithmic form

$$y = \log_3 x$$

$$y = \log_3 x$$

Inverse of  $y = \log_3 x$   
in Exponential form

$$y = 3^x$$

Inverse of  $y = \log_7 x$   
in Exponential form

$$y = \log_7 x$$

$$y = \log_7 x$$

$$y = 7^x$$

These are inverses of each other

**The Key:** You can easily graph a logarithmic equation using the graph of an exponential equation.

## Graph: $y = \log_3 x$

- First graph its inverse ( $y = 3^x$ ) by using a:

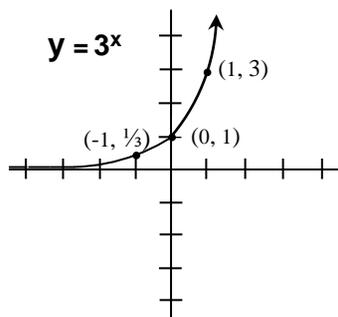
t-chart

or

graphing calculator

x	y
0	1
1	3
-1	$\frac{1}{3}$

Use these ordered pairs to graph  $y = 3^x$



$$y = \boxed{3} \boxed{\wedge} \boxed{x}$$

Enter this into a graphing calculator then go to TABLE to get some ordered pairs.  
(see below)

- If you are using a graphing calculator, go to TABLE and jot down a few ordered pairs:

$(-1, \frac{1}{3})$   $(0, 1)$   $(1, 3)$

x	y1
-1	.33333
0	1
1	3

- Because exponential equations are inverses of logarithm equations, just switch the x's and y's, plot them, and you have graphed a logarithm:

new points:  $(\frac{1}{3}, -1)$   $(1, 0)$   $(3, 1)$

