

Variation Problems

Three Basic Steps

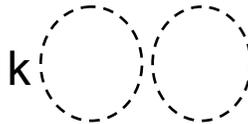
1. Set up the problem as an equation.
2. Solve for "k".
3. Substitute the value of "k" into the Step 1 equation to solve for the new "unknown".

Three Basic Situations

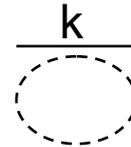
**varies
directly**



**varies
jointly**



**varies
inversely**



Something will go either next to "k" or underneath "k"
(indicating multiplication) (indicating division)

**A variation problem can also include
a *combination* of the three situations:**

"w" varies jointly as "x" and "y", and inversely as "z"

$$W = \frac{K \text{ (x) (y)}}{\text{(z)}}$$

jointly

inversely

Remember!

Note!

Three Steps:

1. Set up an equation
2. Solve for "k"
3. Plug "k" back in

Three Situations:

1. varies directly
 2. varies jointly
 3. varies inversely
- (or some combination)

Varies directly

can be stated as:
directly proportional

Varies inversely

can be stated as:
inversely proportional

Examples:

"y" varies directly as the square of "x" \longrightarrow $y = kx^2$

"n" varies inversely as the square root of "s" \longrightarrow $n = \frac{k}{\sqrt{s}}$

Simple interest varies jointly as principal and time \longrightarrow $I = kpt$
(use "I" for Interest, "p" for principal, and "t" for time)

Word Problem:

The weight of an object on Earth varies directly to that same weight on the moon. If a 210 - pound man would weigh 30 pounds on the moon, how much would a 50 - pound child weigh on the moon?

Step 1:

$$E = km$$

Use "E" for Earth-weight
and "m" for moon-weight.

$$(210) = k(30)$$

Plug in 210 for the man's Earth-weight
and 30 for his moon-weight.

Step 2: $210 = 30k$

Solve for "k" (divide by 30).

$$\frac{210}{30} = \frac{30k}{30}$$

$$k = 7$$

You will always solve for "k" first in variation
problems, and then plug it back into the formula
to solve for the final question (m, in this case).

Step 3: $(50) = (7)m$

Using your original formula, $E = km$, substitute
the value 7 for k, and 50 for the child's Earth-
weight to solve the child's moon-weight.

$$\frac{50}{7} = \frac{7m}{7}$$

$$m = 7.14$$

A child on the moon would weigh about 7.14 pounds.