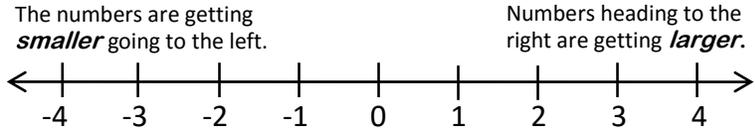


# Graphing One Variable (& Compound) Inequalities

Consider the number line:



The arrows on the number line match the direction of the inequality symbols: Less than ( $<$ ) faces the same way as the smaller numbers, and greater than ( $>$ ) faces the same way as the larger ones.

## Inequality Symbols

Greater than:  $>$

For example,  $13 > -4$   
Thirteen is greater than negative four.

Less than:  $<$

For example,  $-3 < 9$   
Negative three is less than 9.

Greater than or equal to:  $\geq$

For example,  $6 \geq 6$   
Six is greater than **or** equal to six.  
6 is larger than 6 **or** 6 is equal to 6  
(not true) (true)

Less than or equal to:  $\leq$

For example,  $9 \leq 10$   
Nine is less than **or** equal to ten.  
9 is less than 10 **or** 9 is equal to 10  
(true) (not true)

## Solving an Inequality

Solve as an equation:  $-2x < -10$

$$\frac{-2x}{-2} > \frac{-10}{-2}$$

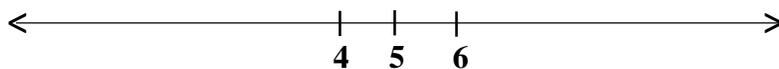
The solution:  $x > 5$   
x is greater than 5

Solve as you would any equation, but keep the inequality sign. Use normal rules of algebra, such as dividing both sides of the inequality by -2.

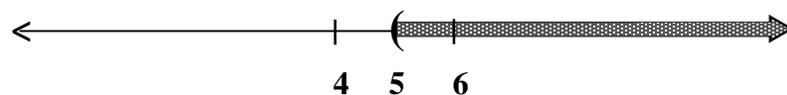
**Note:** When dividing or multiplying by a *negative* number only, the inequality symbol flips to the *opposite* symbol.

## Graphing an Inequality

Graph the solution:  $x > 5$



1. Place the number 5 on the number line.



2. Shade all values greater than 5.

We place a left parenthesis at 5, indicating that the value 5 makes the statement " $x > 5$ " false. This and other graphing symbols are explained in the next portion of this handout.

# Graphing One Variable (& Compound) Inequalities

## Other Important Symbols

In some graphs,  $>$  is represented by  
 $($  or  $\circ$   
 a left parenthesis      an open circle

In some graphs,  $<$  is represented by  
 $)$  or  $\circ$   
 a right parenthesis      an open circle

Left or right parentheses, or an open circle, tell us the value is not part of the solution set.

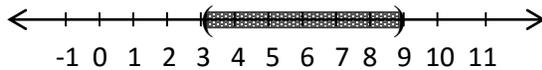
In some graphs,  $\geq$  is represented by  
 $[$  or  $\bullet$   
 a left bracket      a solid circle

In some graphs,  $\leq$  is represented by  
 $]$  or  $\bullet$   
 a right bracket      a solid circle

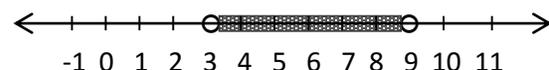
Left or right brackets, or a solid circle, tell us the value is included in the solution set.

## Compound Inequalities

Sometimes, more than one inequality is described in the same expression. For example, when we want to say the solutions include all values between, but not including, 3 and 9, we could say that  $x > 3$  and  $x < 9$ . A more compact expression for this is  $3 < x < 9$ . This *compound inequality* can be graphed in the following ways.

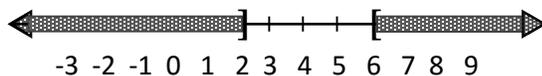


$3 < x < 9$  using parentheses

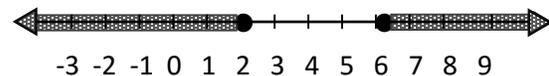


$3 < x < 9$  using open circles

If a compound inequality uses the word “or” instead of “and”, the graph may have two shaded areas, representing the two parts of the expression. Here we graph  $x \leq 2$  or  $x \geq 6$ .



$x \leq 2$  or  $x \geq 6$  using brackets



$x \leq 2$  or  $x \geq 6$  using solid circles

## A Few Words About Interval Notation

Brackets and parentheses are also used in *interval notation*, which identifies the values in the solution set. For example, when  $x > 3$  and  $x < 9$ , we would write that the solution set consists of the interval  $(3,9)$ . As before, brackets or parentheses tell us whether the value is included in or excluded from the solution set. So if  $x > -2$  and  $x \leq 8$ , the solution set would be written as  $(-2,8]$  in interval notation. This tells us that  $-2$  is excluded and  $8$  is included.